

Two-Way ANOVA

R Handout

Derek H. Ogle

```
> library(NCStats)
> library(multcomp)      # glht()
```

Bacteria Example

Background

What is the optimal temperature (27,35,43C) and concentration (0.6,0.8,1.0,1.2,1.4% by weight) of the nutrient, tryptone, for culturing the *Staphylococcus aureus* bacterium. Each treatment was repeated twice. The number of bacteria was recorded in millions CFU/mL (CFU=Colony Forming Units).

```
> setwd("C:/aaaWork/Web/GitHub/NCMTH207/modules/Anova-2Way")
> bact <- read.csv("Bacteria.csv")
> str(bact)
```

```
'data.frame':  30 obs. of  3 variables:
 $ temp : int  27 27 27 27 27 35 35 35 35 35 ...
 $ conc  : num  0.6 0.8 1 1.2 1.4 0.6 0.8 1 1.2 1.4 ...
 $ cells: int  55 120 186 260 151 82 166 179 223 178 ...
```

```
> bact$temp <- factor(bact$temp)
> bact$conc <- factor(bact$conc)
```

```
> ylbl <- "Mean Number of Cells"
> conclbl <- "Concentration (%)"
> templbl <- "Temperature (C)"
```

Initial Summaries

```
> sumTable(cells~temp*conc,data=bact,FUN=length)
```

```
      0.6 0.8 1 1.2 1.4
27    2  2  2  2  2
35    2  2  2  2  2
43    2  2  2  2  2
```

```
> sumTable(cells~temp*conc,data=bact,FUN=mean,digits=0)
```

```
      0.6 0.8  1 1.2 1.4
27  102 106 160 267 131
35   88 161 170 230 198
43  134 166 136 208 164
```

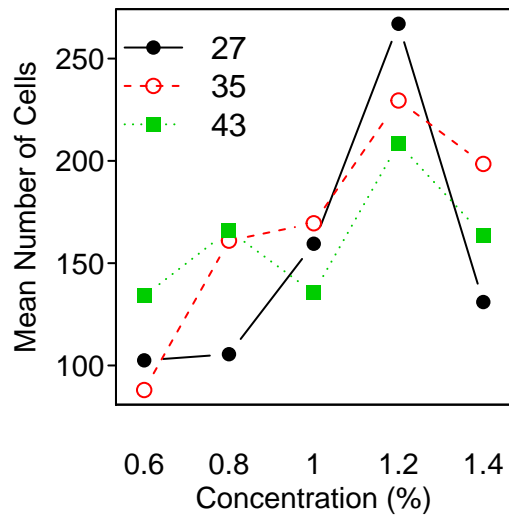
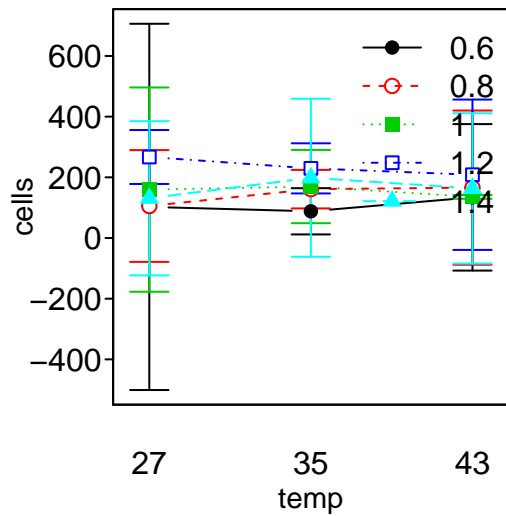
Model Fitting and Summary

```
> lm1 <- lm(cells~temp*conc,data=bact)
> anova(lm1)
```

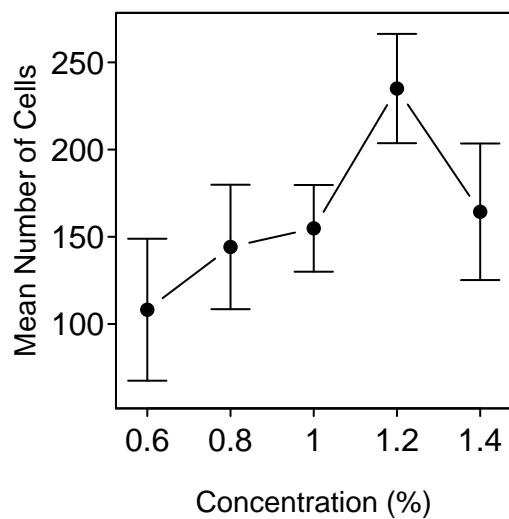
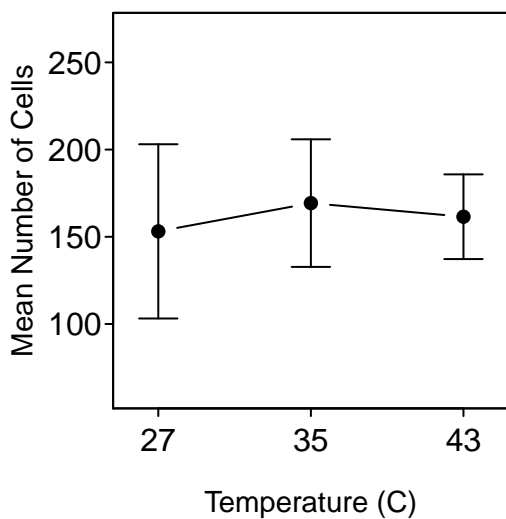
Analysis of Variance Table

```
Response: cells
      Df Sum Sq Mean Sq F value    Pr(>F)
temp    2  1313   656.4  0.8557  0.44473
conc    4 51596 12899.1 16.8154 2.041e-05
temp:conc 8 14703  1837.8  2.3958  0.06886
Residuals 15 11507   767.1
```

```
> fitPlot(lm1) # left
> fitPlot(lm1,interval=FALSE,change.order=TRUE,xlab=conclbl,ylab=ylbl,legend="topleft")
```



```
> fitPlot(lm1,which="temp",ylim=c(60,270),xlab=templbl,ylab=ylbl) # left
> fitPlot(lm1,which="conc",ylim=c(60,270),xlab=conclbl,ylab=ylbl)
```



Multiple Comparisons

```
> bact.mc1 <- glht(lm1, mcp(conc="Tukey"))
```

Warning in mcp2matrix(model, linfct = linfct): covariate interactions found -- default contrast might be inappropriate

```
> summary(bact.mc1)
```

Simultaneous Tests for General Linear Hypotheses

Multiple Comparisons of Means: Tukey Contrasts

Fit: $\text{lm}(\text{formula} = \text{cells} \sim \text{temp} * \text{conc}, \text{data} = \text{bact})$

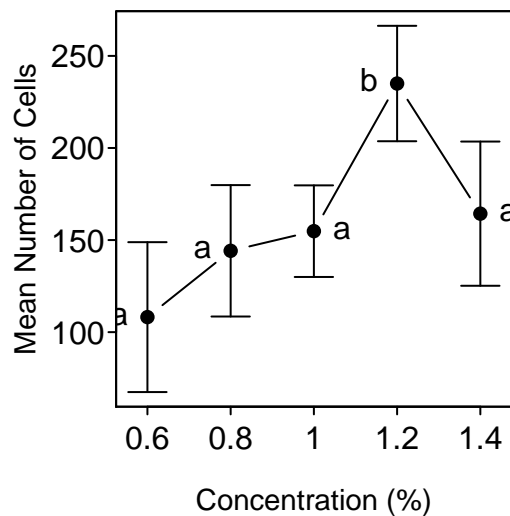
Linear Hypotheses:

	Estimate	Std. Error	t value	Pr(> t)
0.8 - 0.6 == 0	3.0	27.7	0.108	0.999965
1 - 0.6 == 0	57.0	27.7	2.058	0.287167
1.2 - 0.6 == 0	164.5	27.7	5.939	0.000249
1.4 - 0.6 == 0	28.5	27.7	1.029	0.838171
1 - 0.8 == 0	54.0	27.7	1.950	0.334983
1.2 - 0.8 == 0	161.5	27.7	5.831	0.000280
1.4 - 0.8 == 0	25.5	27.7	0.921	0.884532
1.2 - 1 == 0	107.5	27.7	3.881	0.010991
1.4 - 1 == 0	-28.5	27.7	-1.029	0.838185
1.4 - 1.2 == 0	-136.0	27.7	-4.910	0.001448

(Adjusted p values reported -- single-step method)

```
> fitPlot(lm1, which="conc", xlab="conclbl", ylab="yblbl")
```

```
> addSigLetters(lm1, which="conc", lets=c("a", "a", "a", "b", "a"), pos=c(2,2,4,2,4))
```



Soil Phosphorous Example

Background

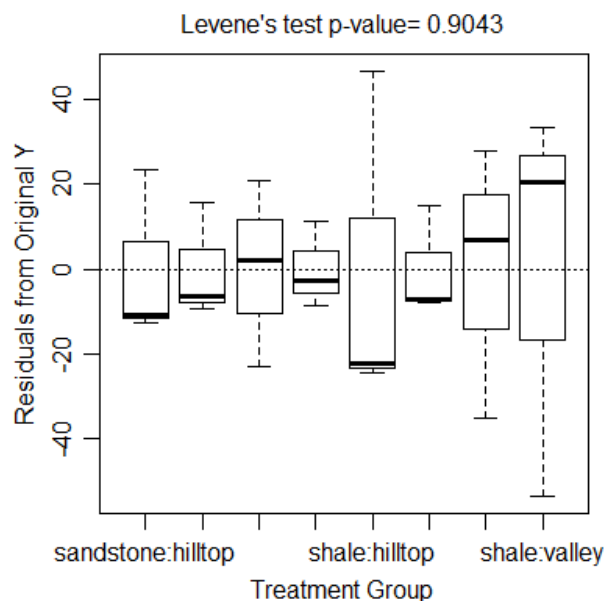
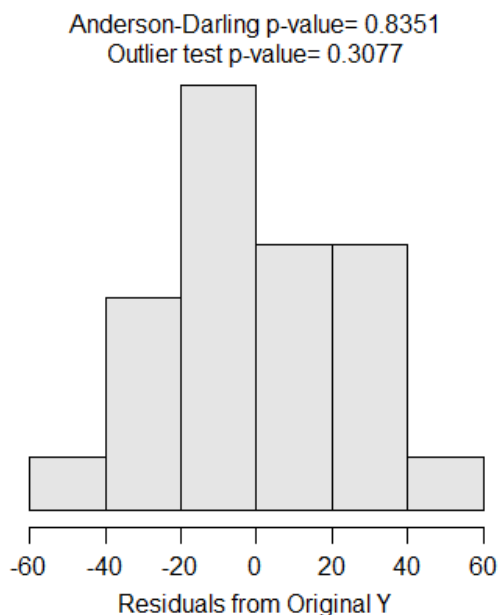
Soil phosphorous is important for the invasion of native vegetation by exotic weeds. Clements (1983) studied the soil phosphorous in the Sydney region (Australia) to determine how soil phosphorous varied with topographical location and soil type. Bushland sites were chosen in Brisbane Waters National Park, Ku-ring-gai Chase National Park and Royal National Park. These areas were relatively unaffected by suburban development, were free from immediate roadside or track effects, and had not been burned for at least two years. Shale-derived and sandstone-derived soils in four topographic locations were examined with three 250 m² quadrats in each of the eight combinations of soil type and topography. Cores of soil of 75 mm depth and 25 mm diameter, free from surface litter, were collected from each of five randomly selected points in each quadrat. The five soil samples were pooled and the total soil phosphorous (ppm) was determined for each pooled sample. Determine the effect of soil type and topography on total soil phosphorous level.

```
> sp <- read.csv("SoilPhosphorous.csv")
> str(sp)
```

```
'data.frame': 24 obs. of 3 variables:
 $ soil: Factor w/ 2 levels "sandstone","shale": 2 2 2 2 2 2 2 2 2 2 ...
 $ topo: Factor w/ 4 levels "hilltop","north",...: 4 4 4 2 2 2 3 3 3 1 ...
 $ phos: int 98 172 185 78 77 100 117 54 96 83 ...
```

Analysis

```
> lm1 <- lm(phos~soil*topo,data=sp)
> transChooser(lm1)
```



```
> anova(lm1)
```

Analysis of Variance Table

Response: phos

```

      Df Sum Sq Mean Sq F value    Pr(>F)
soil    1 17876.0 17876.0 22.9818 0.0001988
topo    3  9693.8  3231.3  4.1542 0.0235128
soil:topo 3 11390.8  3796.9  4.8814 0.0134826
Residuals 16 12445.3    777.8

```

```

> sp$comb <- sp$soil:sp$topo
> view(sp)

```

```

      soil    topo phos      comb
3    shale valley 185  shale:valley
6    shale  north 100  shale:north
10   shale hilltop 83  shale:hilltop
18 sandstone  north 24  sandstone:north
19 sandstone  south 28  sandstone:south
23 sandstone hilltop 21 sandstone:hilltop

```

```

> lm1a <- lm(phos~comb,data=sp)
> anova(lm1a)

```

Analysis of Variance Table

Response: phos

```

      Df Sum Sq Mean Sq F value    Pr(>F)
comb    7 38961  5565.8  7.1555 0.0005729
Residuals 16 12445    777.8

```

```

> spint.mc <- glht(lm1a, mcp(comb="Tukey"))

```

```

> summary(spint.mc)

```

Simultaneous Tests for General Linear Hypotheses

Multiple Comparisons of Means: Tukey Contrasts

Fit: lm(formula = phos ~ comb, data = sp)

Linear Hypotheses:

	Estimate	Std. Error	t value	Pr(> t)
sandstone:north - sandstone:hilltop == 0	1.667	22.772	0.073	1.000
sandstone:south - sandstone:hilltop == 0	19.333	22.772	0.849	0.987
sandstone:valley - sandstone:hilltop == 0	-4.000	22.772	-0.176	1.000
shale:hilltop - sandstone:hilltop == 0	4.667	22.772	0.205	1.000
shale:north - sandstone:hilltop == 0	53.333	22.772	2.342	0.331
shale:south - sandstone:hilltop == 0	57.333	22.772	2.518	0.255
shale:valley - sandstone:hilltop == 0	120.000	22.772	5.270	<0.01
sandstone:south - sandstone:north == 0	17.667	22.772	0.776	0.992
sandstone:valley - sandstone:north == 0	-5.667	22.772	-0.249	1.000
shale:hilltop - sandstone:north == 0	3.000	22.772	0.132	1.000
shale:north - sandstone:north == 0	51.667	22.772	2.269	0.366
shale:south - sandstone:north == 0	55.667	22.772	2.445	0.285
shale:valley - sandstone:north == 0	118.333	22.772	5.196	<0.01
sandstone:valley - sandstone:south == 0	-23.333	22.772	-1.025	0.963
shale:hilltop - sandstone:south == 0	-14.667	22.772	-0.644	0.997

shale:north - sandstone:south == 0	34.000	22.772	1.493	0.800
shale:south - sandstone:south == 0	38.000	22.772	1.669	0.705
shale:valley - sandstone:south == 0	100.667	22.772	4.421	<0.01
shale:hilltop - sandstone:valley == 0	8.667	22.772	0.381	1.000
shale:north - sandstone:valley == 0	57.333	22.772	2.518	0.255
shale:south - sandstone:valley == 0	61.333	22.772	2.693	0.194
shale:valley - sandstone:valley == 0	124.000	22.772	5.445	<0.01
shale:north - shale:hilltop == 0	48.667	22.772	2.137	0.434
shale:south - shale:hilltop == 0	52.667	22.772	2.313	0.344
shale:valley - shale:hilltop == 0	115.333	22.772	5.065	<0.01
shale:south - shale:north == 0	4.000	22.772	0.176	1.000
shale:valley - shale:north == 0	66.667	22.772	2.928	0.131
shale:valley - shale:south == 0	62.667	22.772	2.752	0.176

(Adjusted p values reported -- single-step method)

```
> glhtSig(spint.mc)
```

```
[1] "shale:valley - sandstone:hilltop" "shale:valley - sandstone:north"
[3] "shale:valley - sandstone:south"   "shale:valley - sandstone:valley"
[5] "shale:valley - shale:hilltop"
```

```
> fitPlot(lm1,change.order=TRUE,interval=FALSE,main="",ylim=c(20,160),
          ylab="Mean Phosphorous Level",xlab="Topographic Location",legend="topleft")
> addSigLetters(lm1,change.order=TRUE,lets=c("a","a","a","ab","a","ab","a","b"),
               pos=c(1,3,1,3,1,1,3,1))
```

